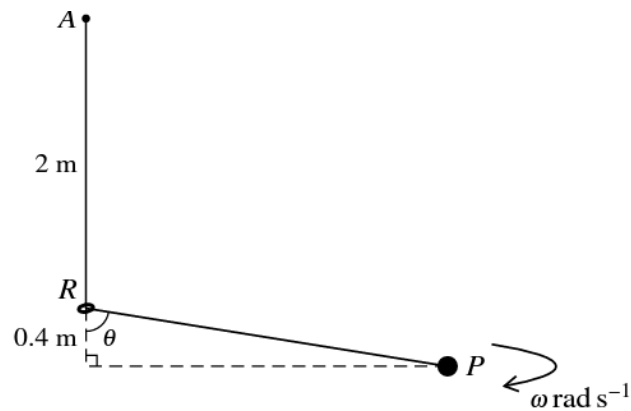


Circular Motion 2

Q1.



One end of a light elastic string with modulus of elasticity 15 N is attached to a fixed point A which is 2 m vertically above a fixed small smooth ring R . The string has natural length 2 m and it passes through R . The other end of the string is attached to a particle P of mass m kg which moves with constant angular speed $\omega \text{ rad s}^{-1}$ in a horizontal circle which has its centre 0.4 m vertically below the ring. PR makes an acute angle θ with the vertical (see diagram).

(i) Show that the tension in the string is $\frac{3}{\cos \theta}$ N and hence find the value of m . [4]

(ii) Show that the value of ω does not depend on θ . [4]

It is given that for one value of θ the elastic potential energy stored in the string is twice the kinetic energy of P .

(iii) Find this value of θ . [4]

Q2.

A horizontal disc with a rough surface rotates about a fixed vertical axis which passes through the centre of the disc. A particle P of mass 0.2 kg is in contact with the surface and rotates with the disc, without slipping, at a distance 0.5 m from the axis. The greatest speed of P for which this motion is possible is 1.5 m s^{-1} .

(i) Calculate the coefficient of friction between the disc and P . [2]

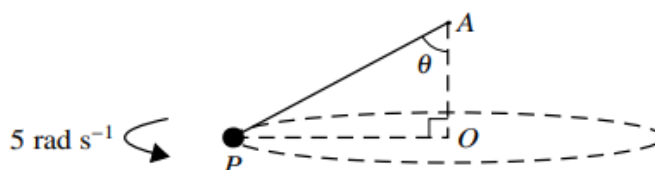
P is now attached to one end of a light elastic string, which is connected at its other end to a point on the vertical axis above the disc. The tension in the string is equal to half the weight of P . The disc rotates with constant angular speed $\omega \text{ rad s}^{-1}$ and P rotates with the disc without slipping. P moves in a circle of radius 0.5 m, and the taut string makes an angle of 30° with the horizontal.

(ii) Find the greatest and least values of ω for which this motion is possible. [5]

(iii) Calculate the value of ω for which the disc exerts no frictional force on P . [2]

Circular Motion 2

Q3.



One end of a light inextensible string is attached to a fixed point A and the other end of the string is attached to a particle P . The particle P moves with constant angular speed 5 rad s^{-1} in a horizontal circle which has its centre O vertically below A . The string makes an angle θ with the vertical (see diagram). The tension in the string is three times the weight of P .

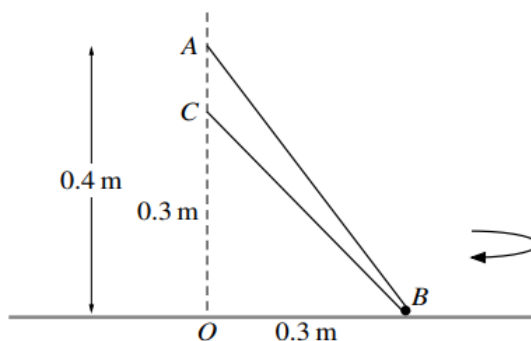
- (i) Show that the length of the string is 1.2 m . [3]
 - (ii) Find the speed of P . [4]
-

Q4.

One end of a light inextensible string of length 0.5 m is attached to a fixed point A . The other end of the string is attached to a particle P of weight 6 N . Another light inextensible string of length 0.5 m connects P to a fixed point B which is 0.8 m vertically below A . The particle P moves with constant speed in a horizontal circle with centre at the mid-point of AB . Both strings are taut.

- (i) Calculate the speed of P when the tension in the string BP is 2 N . [5]
 - (ii) Show that the angular speed of P must exceed 5 rad s^{-1} . [3]
-

Q5.

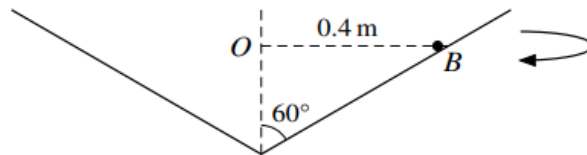


A light inextensible string passes through a small smooth bead B of mass 0.4 kg . One end of the string is attached to a fixed point A 0.4 m above a fixed point O on a smooth horizontal surface. The other end of the string is attached to a fixed point C which is vertically below A and 0.3 m above the surface. The bead moves with constant speed on the surface in a circle with centre O and radius 0.3 m (see diagram).

Circular Motion 2

- (i) Given that the tension in the string is 2 N, calculate
- (a) the angular speed of the bead, [3]
- (b) the magnitude of the contact force exerted on the bead by the surface. [2]
- (ii) Given instead that the bead is about to lose contact with the surface, calculate the speed of the bead. [4]
-

Q6.



A small ball B of mass 0.5 kg moves in a horizontal circle with centre O and radius 0.4 m on the smooth inner surface of a hollow cone fixed with its vertex down. The axis of the cone is vertical and the semi-vertical angle is 60° (see diagram).

- (i) Show that the magnitude of the force exerted by the cone on B is 5.77 N, correct to 3 significant figures, and calculate the angular speed of B . [4]

One end of a light elastic string of natural length 0.45 m and modulus of elasticity 36 N is attached to B . The other end of the string is attached to the point on the axis 0.3 m above O . The ball B again moves on the surface of the cone in the same horizontal circle as before.

- (ii) Calculate the speed of B . [6]
-

Q7.

A particle P of mass 0.15 kg is attached to one end of a light elastic string of natural length 0.4 m and modulus of elasticity 12 N. The other end of the string is attached to a fixed point A . The particle P moves in a horizontal circle which has its centre vertically below A , with the string inclined at θ° to the vertical and $AP = 0.5$ m.

- (i) Find the angular speed of P and the value of θ . [5]
- (ii) Calculate the difference between the elastic potential energy stored in the string and the kinetic energy of P . [4]
-

Circular Motion 2

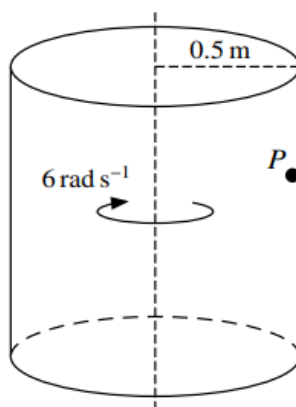
Q8.

A particle P of mass 0.2 kg moves with speed 4 m s^{-1} and angular speed 5 rad s^{-1} in a horizontal circle on a smooth surface. P is attached to one end of a light elastic string of natural length 0.6 m . The other end of the string is attached to the point on the surface which is the centre of the circular motion of P .

(i) Find the radius of this circle. [1]

(ii) Find the modulus of elasticity of the string. [4]

Q9.



A hollow cylinder with a rough inner surface has radius 0.5 m . A particle P of mass 0.4 kg is in contact with the inner surface of the cylinder. The particle and cylinder rotate together with angular speed 6 rad s^{-1} about the vertical axis of the cylinder, so that the particle moves in a horizontal circle (see diagram). Given that P is about to slip downwards, find the coefficient of friction between P and the surface of the cylinder. [4]
